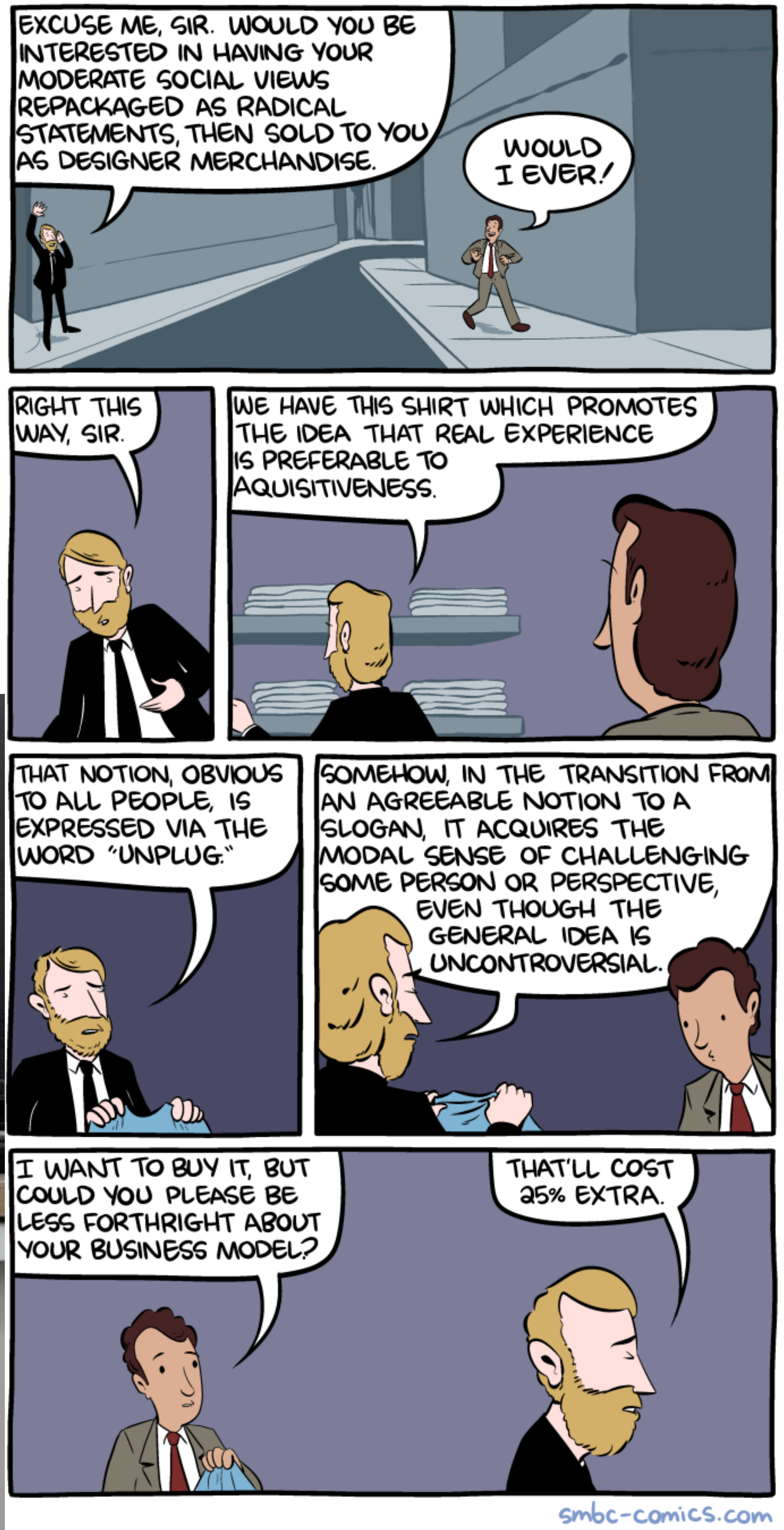
Test Suite Quality Metrics


EXCUSE ME, SIR. WOULD YOU BE INTERESTED IN HAVING YOUR MODERATE SOCIAL VIEWS REPACKAGED AS RADICAL STATEMENTS, THEN SOLD TO YOU AS DESIGNER MERCHANDISE.
WOULD I EVER!
RIGHT THIS WAY, SIR.
WE HAVE THIS SHIRT WHICH PROMOTES THE IDEA THAT REAL EXPERIENCE IS PREFERABLE TO AQUISITIVENESS.
THAT NOTION, OBVIOUS TO ALL PEOPLE, IS EXPRESSED VIA THE WORD "UNPLUG."
SOMEHOW, IN THE TRANSITION FROM AN AGREEABLE NOTION TO A SLOGAN, IT ACQUIRES THE MODAL SENSE OF CHALLENGING SOME PERSON OR PERSPECTIVE, EVEN THOUGH THE GENERAL IDEA IS UNCONTROVERSIAL.
I WANT TO BUY IT, BUT COULD YOU PLEASE BE LESS FORTHRIGHT ABOUT YOUR BUSINESS MODEL?
THAT'LL COST 25% EXTRA.
smbc-comics.com

Review: Quality Assurance

- We use **testing** to help assure the quality of software we deliver
- Testing consists of **running the subject program** on a subset of possible **inputs**, comparing results or behavior to a known **output**
- Your test suite represents the *specification* for the program
- Testing gives you *confidence* (not proof) that the program **does** some **good** things and **doesn’t** do some **bad** things
  - Testing is imperfect: proving programs are correct is undecidable

Review: Testing Concepts

- **Regression** testing helps detect regressions in software
- **Fuzz** testing helps automate the process of selecting inputs
- **Penetration** testing helps discover security vulnerabilities
- **Unit** tests evaluate individual components
- **Integration** tests evaluate the **end-to-end** system
  - The divide between unit and integration testing is blurry
    - Unit tests that depend on external components could be thought of as integrations
    - Generally, Unit tests are for very specific behavior (other components are black-boxed)
- **Mocking** helps make testing **cheaper**

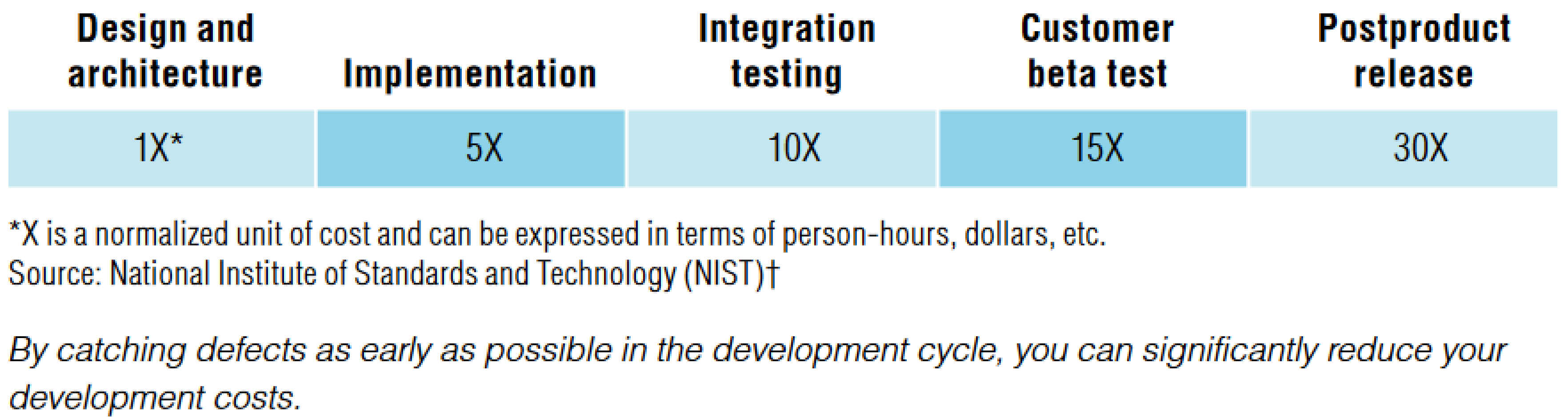
One-Slide Summary

- **Test suite quality metrics** help us decide which suite to use. **Line coverage**, the fraction of lines visited when running a suite, is simple but gives limited confidence. **Branch coverage**, which requires both true and false values for conditionals, is richer (incorporating data values indirectly). **Mutation analysis** measures the fraction of seeded defects detected by a suite; it is expensive but effective.
- **Beta** and **A/B testing** involve real users and their experiences.

Somehow, Testing returned.

The Story So Far …

- **Testing** is the most common dynamic technique for software quality assurance.
- Testing is very expensive (e.g., 35% of total IT spending).
  [Capgemini World Quality Report. 2015]
- Not testing, or testing badly, is even more expensive
  [Minimizing code defects to improve software quality and lower development costs. IBM 2008]



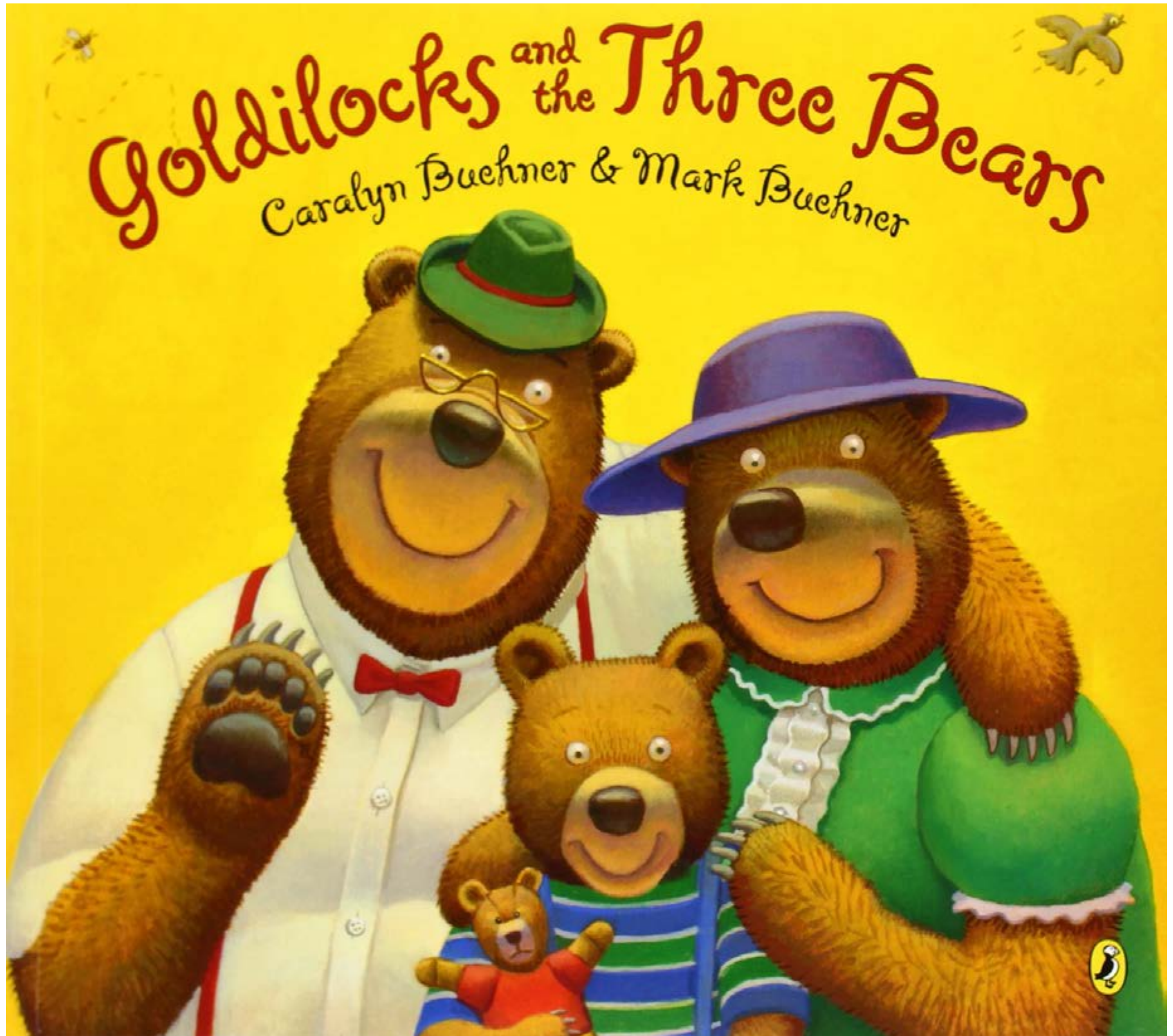
Design and architecture	Implementation	Integration testing	Customer beta test	Postproduct release
1X*	5X	10X	15X	30X

*X is a normalized unit of cost and can be expressed in terms of person-hours, dollars, etc.
Source: National Institute of Standards and Technology (NIST)†

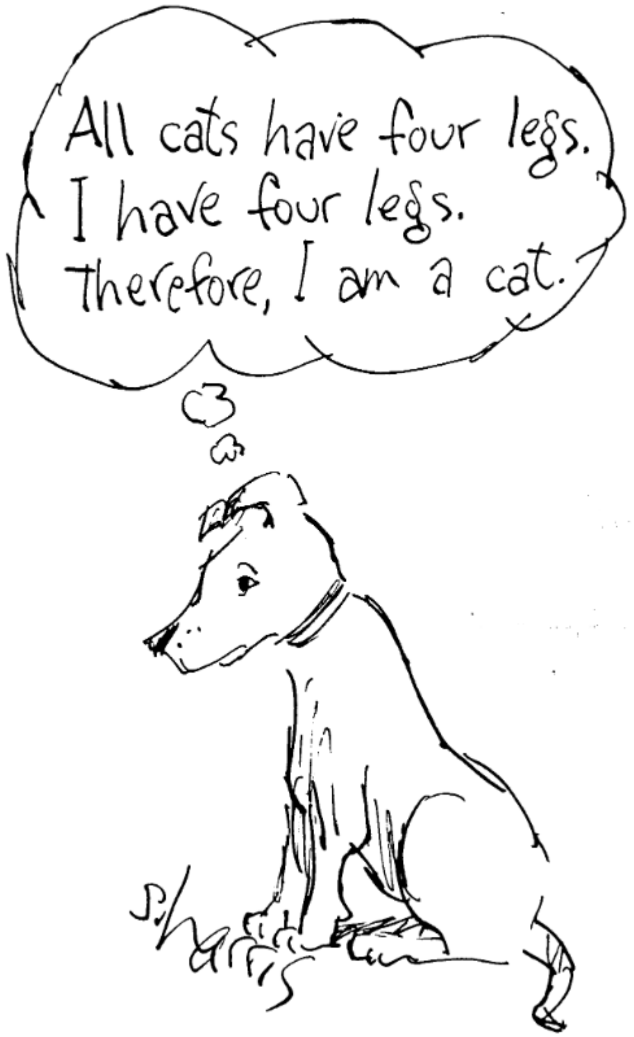
By catching defects as early as possible in the development cycle, you can significantly reduce your development costs.

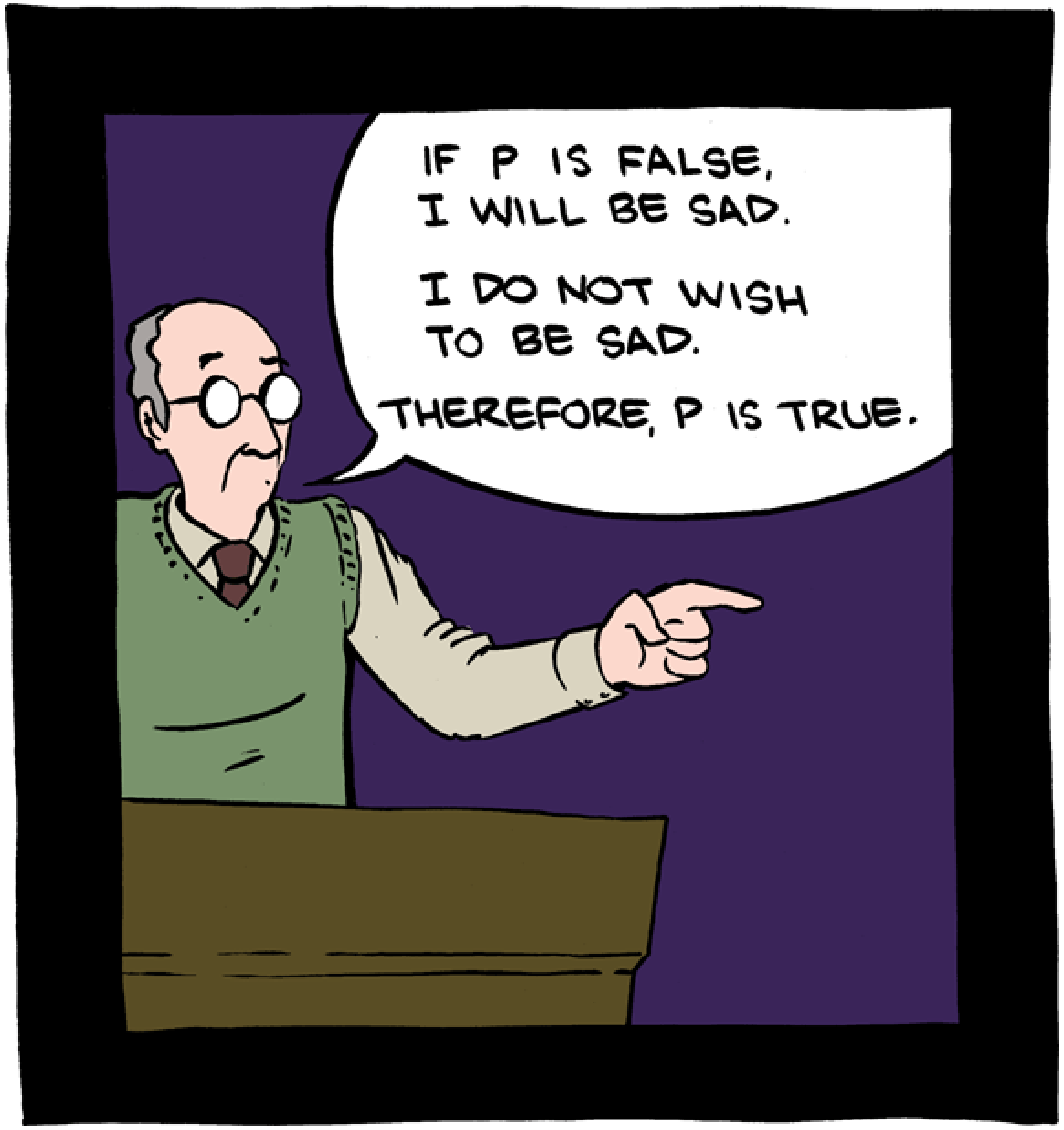
Guiding Narrative

- How should we think about testing?
- Lens of **Logic**
- Lens of **Statistics**
- Lens of **Adversity**


Goldilocks and the Three Bears
Caralyn Buchner & Mark Buchner

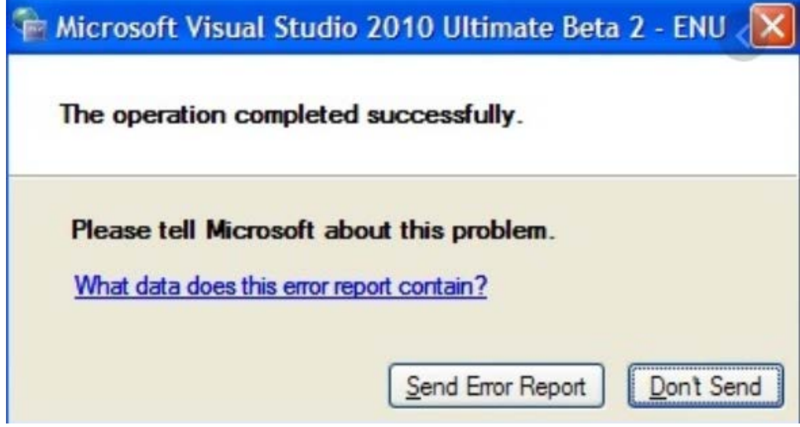
Lens of Logic





There. Now you can skip 99% of philosophical debates.

The Motivation


Microsoft Visual Studio 2010 Ultimate Beta 2 - ENU

The operation completed successfully.

Please tell Microsoft about this problem.

What data does this error report contain?

- If testing is our best way to **gain confidence** in the **quality** of software, but testing is **expensive**, how can we ensure that we are **testing** in an effective manner?

- Informally Want: The program passes the tests if and only if it does all the right things and none of the wrong things.
  - Pass all tests → program adheres to requirements
  - Each failing test → program behaves incorrectly

Intuition

- Suppose you were writing a `sqrt` program and one of the requirements was that it should abort gracefully on *negative inputs*.
- Suppose further that your test suite does not include any negative inputs.
- Can we conclude that passing all of the tests implies adhering to all of the requirements?

Test cannot be started because it already does not exist.

Coverage

- We desire all of the requirements to be covered (“checked”) by the test suite.
- For our purposes, ***X* coverage** is the degree to which *X* is executed/exercised by the test suite.
- Examples:
  - Statement coverage is the fraction of source statements that are executed by the test suite.

Do Tests Cover All Requirements?

- Want: **traceability** between requirements and test cases
- Each test case *annotated* like:
  - "a program that passes *this test* satisfies *requirement X*" or
  - "passing *this test* gives confidence that a program adheres to *requirement Y*"
- Outside of certain industries (e.g., Aerospace), such formal traceability is rare

An Approximation

- We will cover **requirements elicitation** later in this course
- Assume: no formal traceability
- So testing that the program does **all** and **only** the good things that it is **required** to do is not possible
  - (or not feasible)

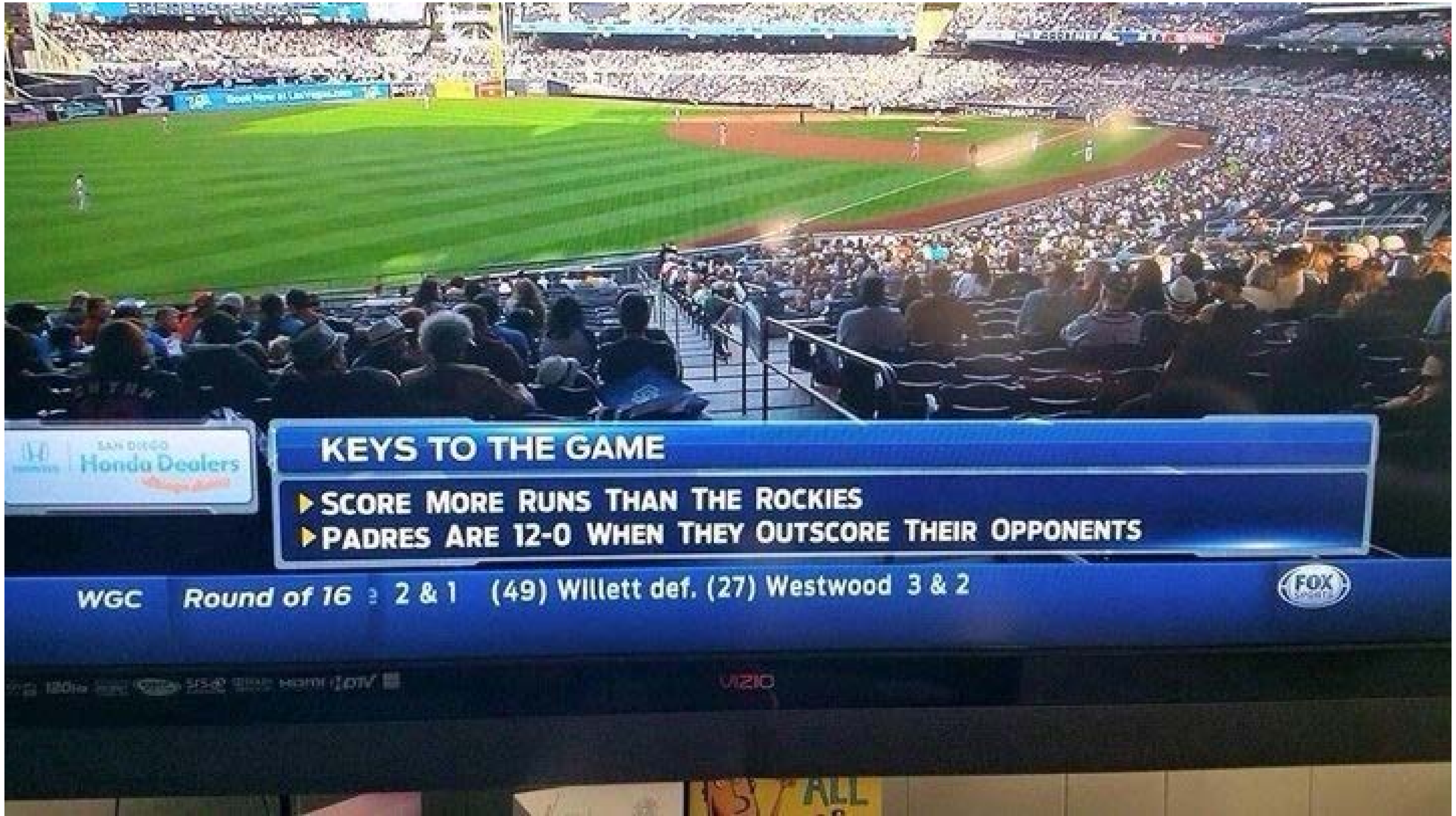
Don't Do Bad Things

- We can at least test that the program does *not* do certain bad things
  - e.g., “don't segfault”,
  - “don't send my password to Microsoft”,
  - “on this one particular input, don't get the wrong answer”
- Note that “I never do bad things” is not the same as “I always/eventually do good things”
  - For more information, take a class on *Modal Logic* or read about *Liveness* vs. *Safety* properties

Testing to Find Bugs

- So now we want to test to gain confidence that the program does not do “bad things”
- That is, that the program does not have bugs
- Key Logical Observation: **If we never test line X then testing cannot rule out the presence of a bug on line X**
- (You could read line X, but we're talking about testing. Later this semester: code review.)

If this seems “too obvious” so far, just wait …


San Diego Honda Dealers
KEYS TO THE GAME
▸SCORE MORE RUNS THAN THE ROCKIES
▸PADRES ARE 12-0 WHEN THEY OUTSCORE THEIR OPPONENTS
WGC Round of 16 2 & 1 (49) Willett def. (27) Westwood 3 & 2
FOX
VIZIO

P → Q

- **“No test covers X → may have a bug in X”**

P → Q

- **“No test covers X → may have a bug in X”**

No test covers X	May have a bug in X
T	T
F	T

“All Other Things Being Equal”

- If test A visits lines 1 and 2
- And test B visits lines 1, 2, 3 and 4
- Then, all other things being equal, we prefer test B
  - Test A gives some confidence about 1 and 2 and no confidence (no information) about 3 and 4
  - Test B gives some confidence about 1, 2, 3 and 4
- If the confidence/info gained per tested line is c>0, test A gives us 2c+0 and test B gives us 4c.
  - Because c>0, we have 4c > 2c. So B > A.

How Does this Square with Unit Testing?

- Earlier we discussed that ideally unit tests cover only one specific functionality
- What if 1 and 2 have different functionality from 3 and 4?
- Ideally:
  - A covers 1,2; B covers 3,4
  - A + B > A
  - Here, “All other things being equal” must hold true ($A \in \{A,B\}$)

Simplifying Assumptions

- Assumption 1. We gain the same amount of confidence (or information) for each visited line.
- Assumption 2. The amount of confidence (or information) we gain per visited line is positive.

Line Coverage: A Test Suite Quality Metric

- A **test suite quality metric** allows test suites to be **compared**.
- **Line (or statement) coverage** is a test suite quality metric: it is the *number of unique lines* (statements) visited (exercised) by the program when *running the test suite*.
  - (Informally: visiting **more** lines is **better** because you gain confidence about visited lines.)

Using Line Coverage

- Given two test suites that both run within your resource budget (“AOTBE”, etc.), if we can only run one, we prefer the test suite with higher line coverage

- Thus coverage is a metric that allows us to compare two test suites and pick the “better” one

- We use this information to guide decision-making in a software process (“how should we do testing?”)

Collecting Line Coverage

- At its simplest, this is just print-statement debugging
- Put a print statement before every line of the program
  - Run all the tests, collect all the printed information, remove duplicates, count
- Practical concern: the **observer effect** (from physics) is the fact that simply observing a situation or phenomenon necessarily changes that phenomenon.

Coverage Instrumentation

- **Coverage instrumentation** modifies a program to record coverage information in a way that minimizes the observer effect.
  - This can be done at the source or binary level.
- Don't actually print to stdout/stderr
- Don't slow things down too much
  - Pre-check before printing a duplicate?
- Don't introduce infinite loops
  - Instrument “print” with a call to “print”?

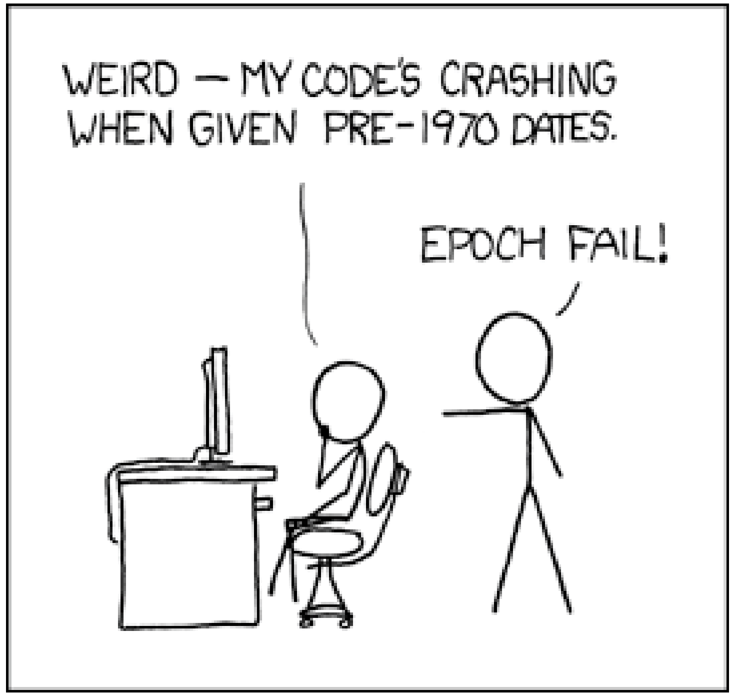
Good News: “Solved” Problem

- This is a well-studied problem and many push-button solutions exist for various forms of coverage
  - Either built in to your IDE or as external tools
- You will use three in the Homework
  - Python's coverage, gcc's gcov, Java's cobertura
- For more information on how to write one yourself, take a (graduate?) PL or Compilers class.

Problems with Line Coverage

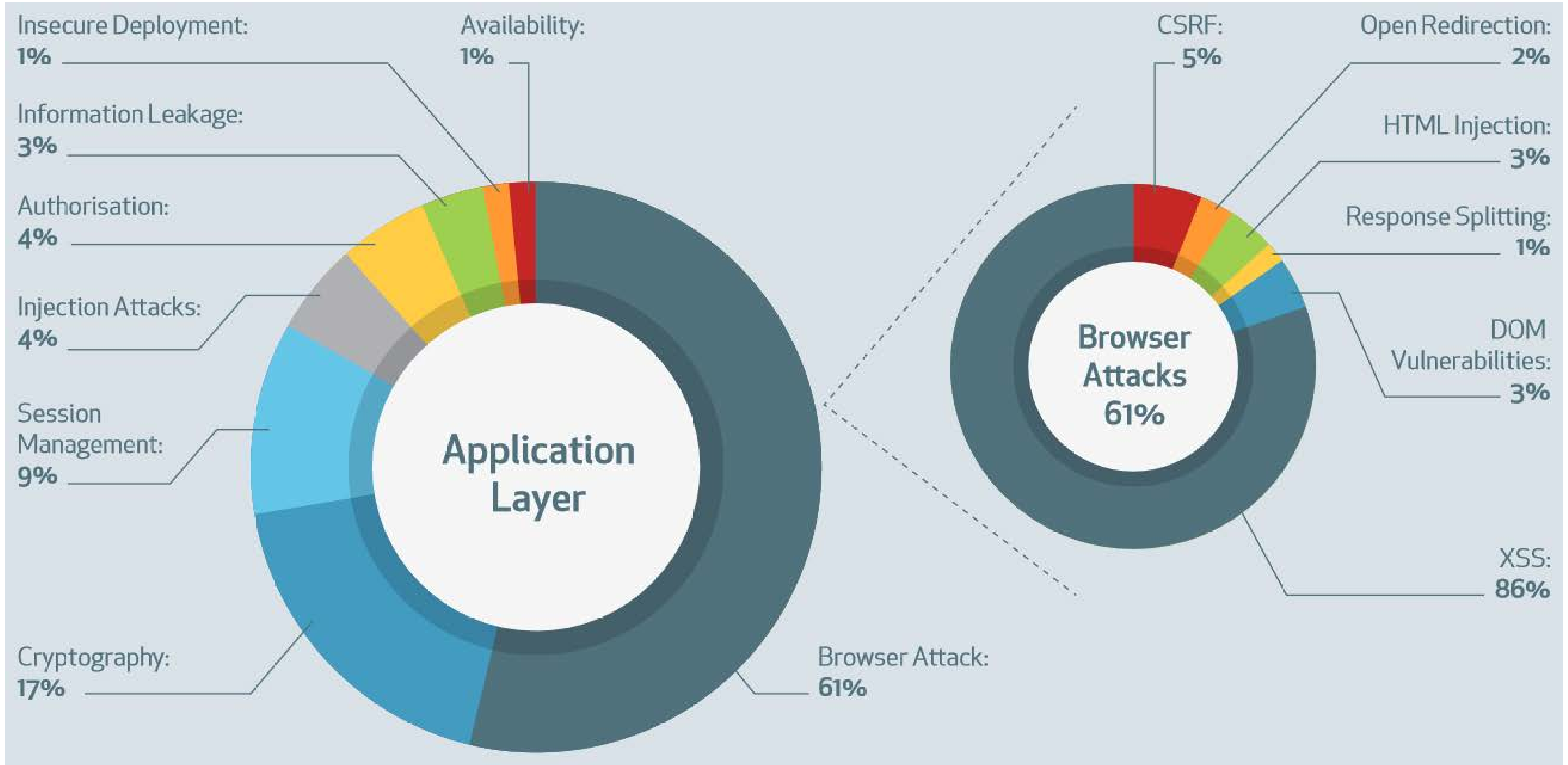
- What could go wrong with line coverage?

- Can you think of situations with 100% line coverage where the program might still have bugs?



Example: Statement Coverage Inadequacy

- Cross-site scripting (XSS) attacks:
  [2016 Vulnerability Statistics Report, edgescan]



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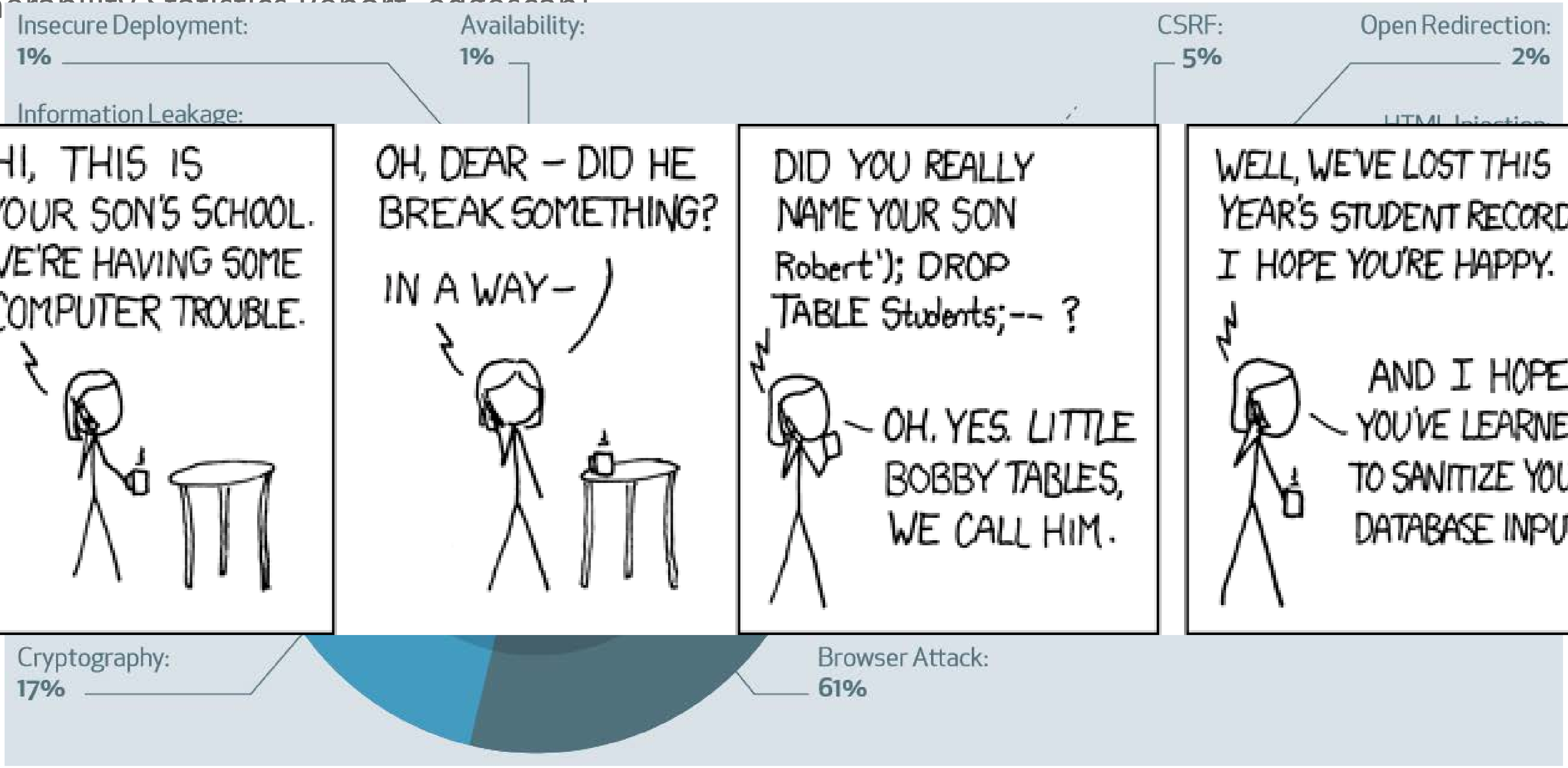
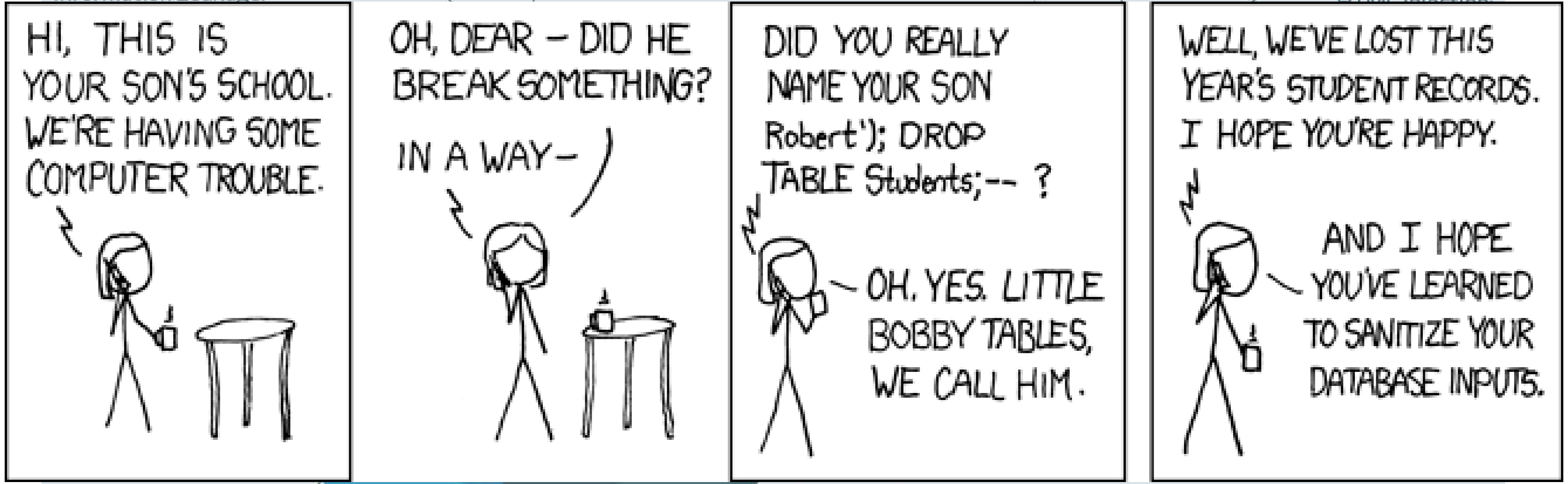
[2016 Vuln




HI, THIS IS YOUR SON'S SCHOOL. WE'RE HAVING SOME COMPUTER TROUBLE.
OH, DEAR – DID HE BREAK SOMETHING?
IN A WAY –
DID YOU REALLY NAME YOUR SON Robert'); DROP TABLE Students;-- ?
OH. YES. LITTLE BOBBY TABLES, WE CALL HIM.
WELL, WE'VE LOST THIS YEAR'S STUDENT RECORDS. I HOPE YOU'RE HAPPY.
AND I HOPE YOU'VE LEARNED TO SANITIZE YOUR DATABASE INPUTS.

Data Values and Implicit Control Flow

- `return a/b`

$\longrightarrow$

```
if (b != 0)
   return a/b;
else
   ABORT
```

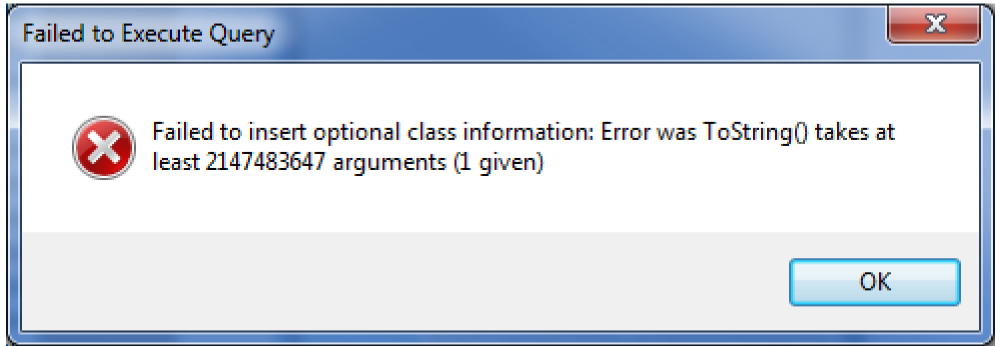
- `print ptr->fld`

$\longrightarrow$

```
if (ptr != NULL)
   print ptr->fld
else
   ABORT
```

Intuition

- Many interesting data values cause *implicit* or *explicit* changes of control
  - That is, they cause different branches of conditionals to execute
- Informally, the problem of ensuring that we cover *interesting data values* may reduce to the problem of ensuring that we cover *all branches of conditionals*


Failed to Execute Query

Failed to insert optional class information: Error was ToString() takes at least 2147483647 arguments (1 given)

Branch Coverage

- **Branch coverage** is a test suite quality metric that counts the total number of conditional branches exercised by that test suite (i.e., if→true and if→false are counted separately)
- Note that branch coverage can subsume line coverage:

```
foo(a):
  if a > 5:
    print “x”
  print “y”
```

What is the line coverage of foo(7)?

How about branch coverage?

Branch Coverage

- **Branch coverage** is a test suite quality metric that counts the total number of conditional branches exercised by that test suite (i.e., if→true and if→false are counted separately)
- Note that branch coverage can subsume line coverage:

```
foo(a):
  if a > 5:
    print “x”
  print “y”
```

Test Suite {foo(7)} has 100% line coverage but 50% branch coverage.

Test Suite {foo(7), foo(0)} has 100% line and 100% branch coverage.

Branch vs. Line

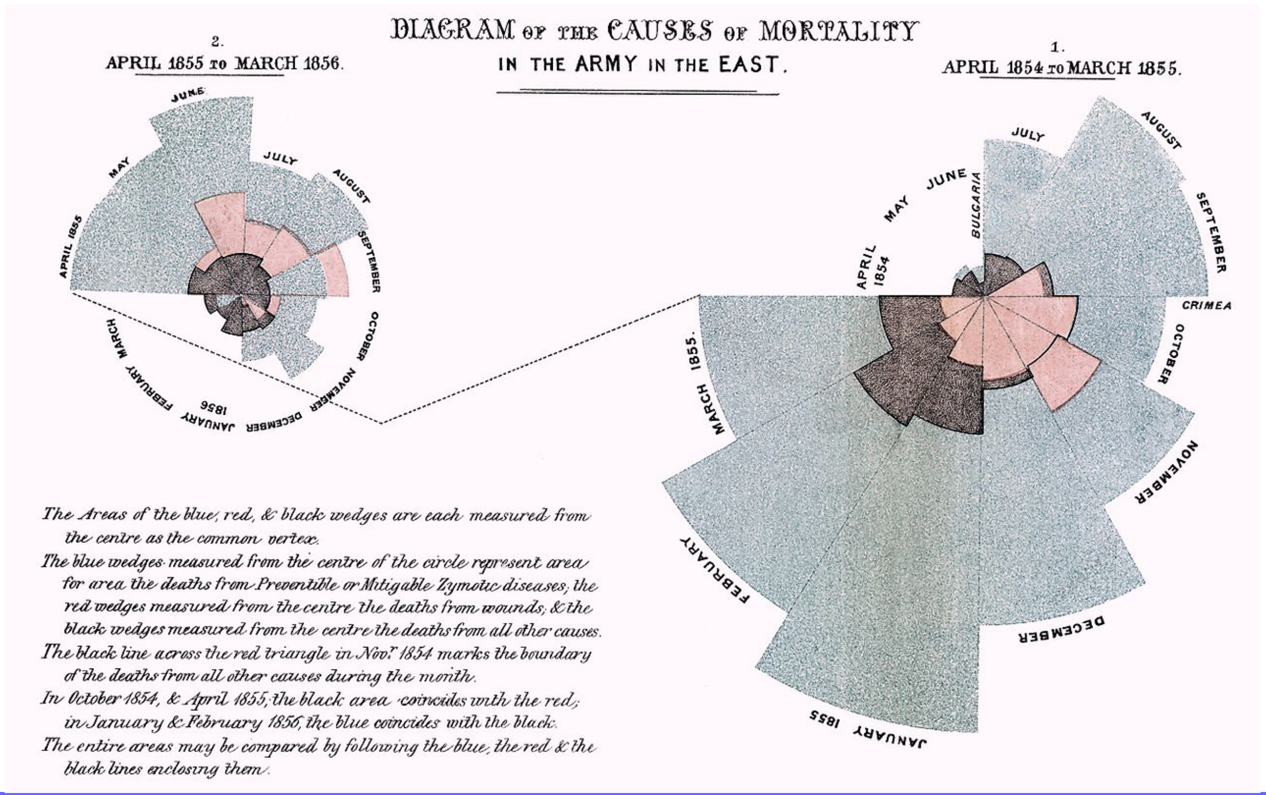
- Branch coverage typically gives us more confidence than line coverage
- *Typically, 100% branch coverage implies 100% line coverage*
- However, branch coverage is “more expensive” in the sense that it is harder for a test suite to have high branch coverage than to have high line coverage
  - Note: quality isn't really “more expensive”, it’s more that line coverage alone isn’t enough. Quality is hard to achieve.

Other Flavors

- **Function Coverage**: what fraction of functions have been called?
- **Condition Coverage**: what fraction of boolean subexpressions have been evaluated?
  - Comparing this to branch coverage is a not-uncommon test question …
- **Modified Condition Coverage (MC/DC)**: branch coverage + independent condition influence (this is a simplification)
  - Used in mission critical (e.g., avionics) software

Trivia: Statistics

- *This* English social reformer and statistician (among other activities, ~1850) was a pioneer in the use of infographics: the effective graphical presentation of statistical data.



The Areas of the blue, red, & black wedges are each measured from the centre as the common vertex.
The blue wedges measured from the centre of the circle represent area for area the deaths from Preventible or Mitigable Zymotic diseases; the red wedges measured from the centre the deaths from wounds; & the black wedges measured from the centre the deaths from all other causes.
The black line across the red triangle in Nov.r 1854 marks the boundary of the deaths from all other causes during the month.
In October 1854, & April 1855; the black area coincides with the red; in January & February 1856, the blue coincides with the black.
The entire areas may be compared by following the blue, the red & the black lines enclosing them.

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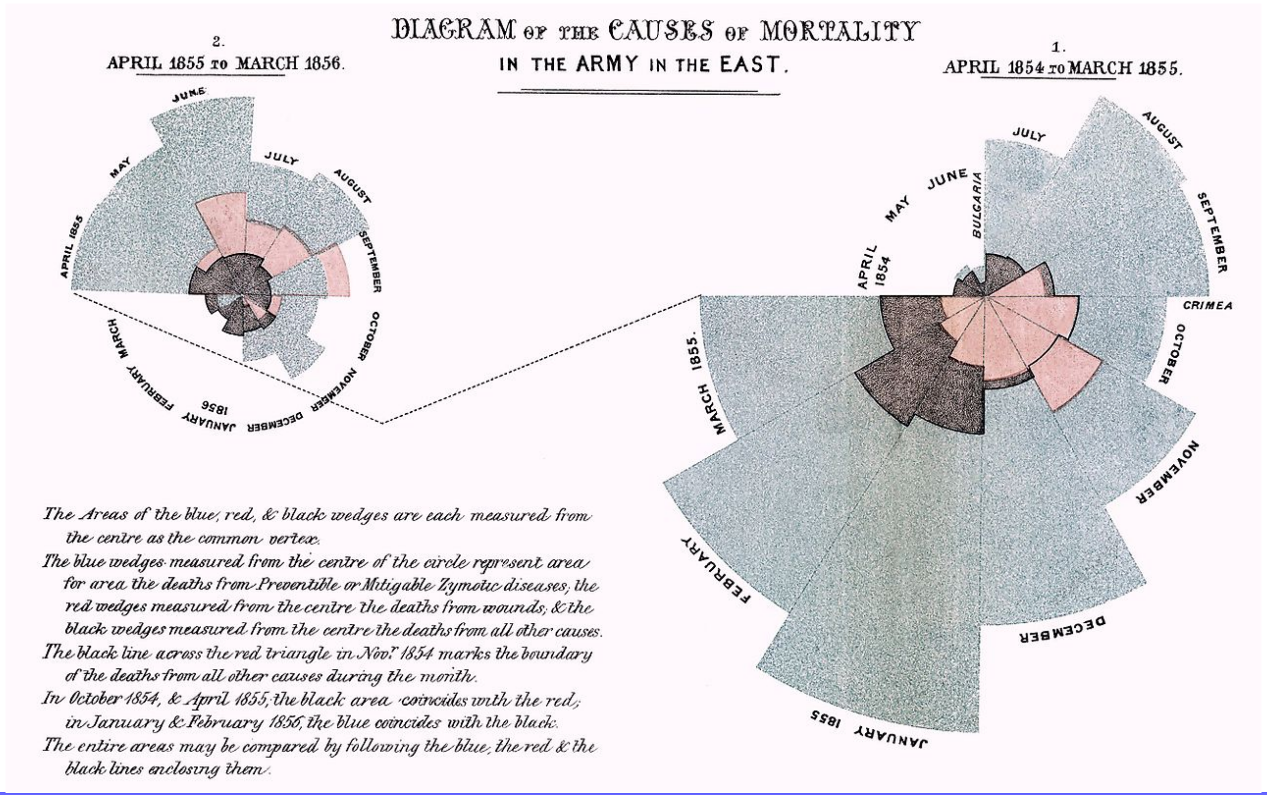

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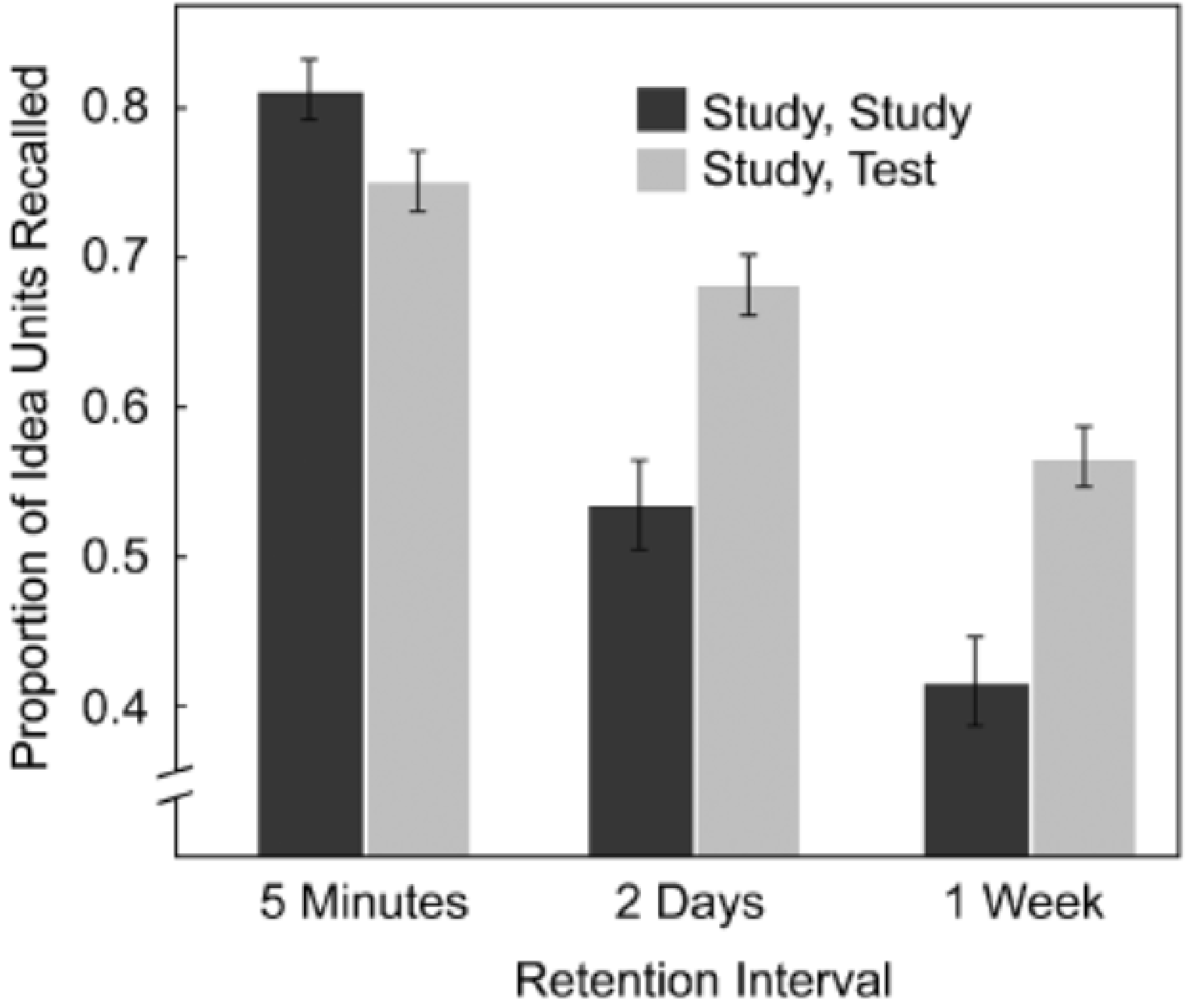
The entire areas may be compared by following the blue, the red & the black lines enclosing them.

Psychology: Recall

- 120 students (age 18 to 24) were asked to study prose passages (e.g., 300 words on “Sea Otters”) and also do math problems
- Group 1: Read for 7m, math for 2m, re-read for 7m, math for 5m
- Group 2: Read for 7m, math for 2m, test for 10m, math for 5m
- Both groups: later → test for 10 minutes
  - Which group did better? By how much?

Psychology: Recall



Psychology: Testing Effect

- The **testing effect**: long-term memory is increased when some of the learning period is devoted to retrieving the to-be-remembered information through testing with feedback.
- “They found that re-studying or re-reading memorized information had no effect, but trying to recall the information had an effect.”
- Implication for SE: Code comprehension.
- [Roediger, H. L.; Karpicke, J. D. (2006). "Test-Enhanced Learning: Taking Memory Tests Improves Long-Term Retention". Psychological Science. 17 (3): 249–255.]

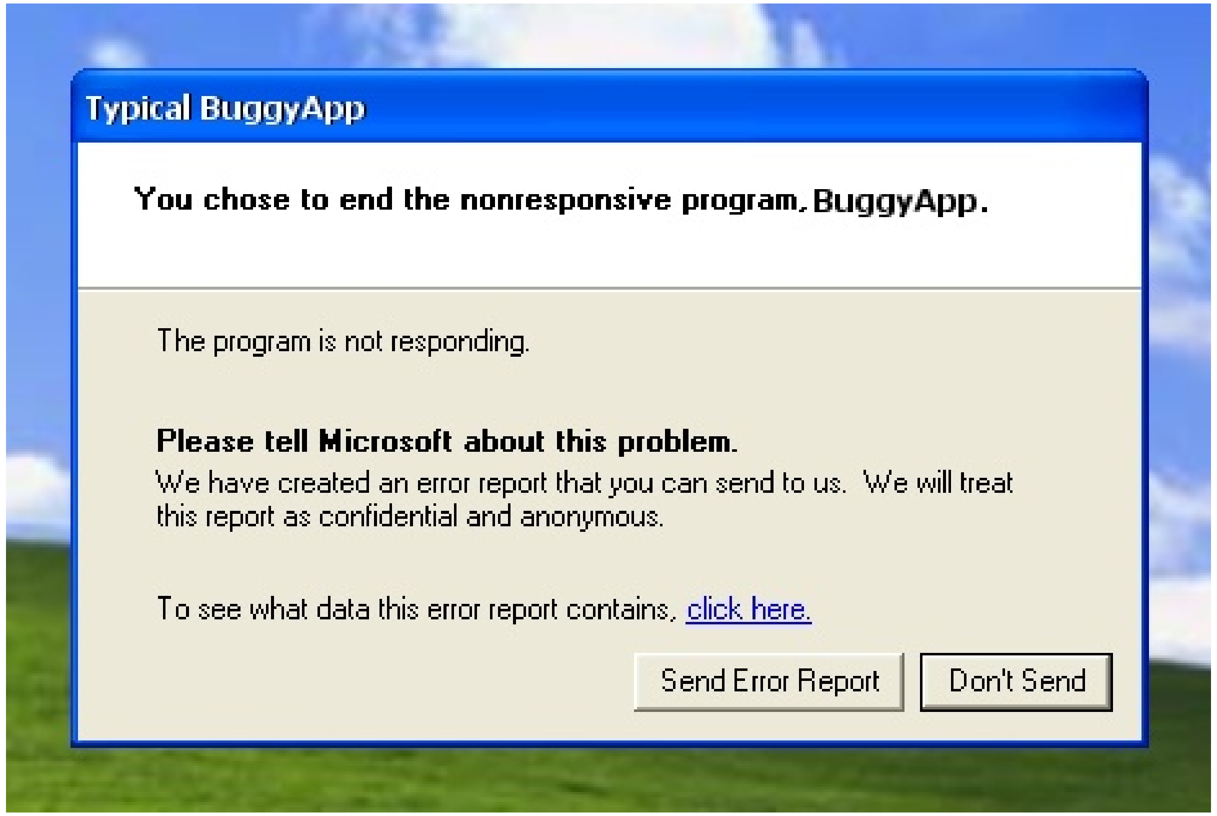
Lens of Statistics

```
Acquiring Fruit. . . . . . . . .
Scanning . . . . . . . . . . . .
Analyzing perimeter:
      ROUND    94.2%
Analyzing color:
     ORANGE    93.7%
Analyzing surface:
     GLOSSY    11.8%

Probability:
      ORANGE 93.231%
```

Alternate View

- The bugs experienced by users are the ones that matter.
- Dually, bugs never experienced by users do not matter.



Typical BuggyApp

You chose to end the nonresponsive program, BuggyApp.

The program is not responding.

Please tell Microsoft about this problem.
We have created an error report that you can send to us. We will treat this report as confidential and anonymous.

To see what data this error report contains, click here.

Positive User View

- Suppose you are writing a cashier application that makes change for a dollar. Given $ between 1 and 100 cents, return the coins to give out as change.
  - e.g., 23 → return 3 quarters and 2 pennies
- In this scenario, you can exhaustively test all 100 inputs that will occur to users in the real world
  - Does it matter if that is 100% coverage
  - (e.g., dead code)

God sending an ionizing particle from outer space to help a mario speedrunner save time

Negative User View

- Suppose users will only ever cause lines 1, 2 and 3 of your program to be executed
- Then you do not need to test line 4
  - Even if it has a bug, users will never encounter that bug

- Note “will” → this either requires either clairvoyance or a finite input domain

Testing as Sampling

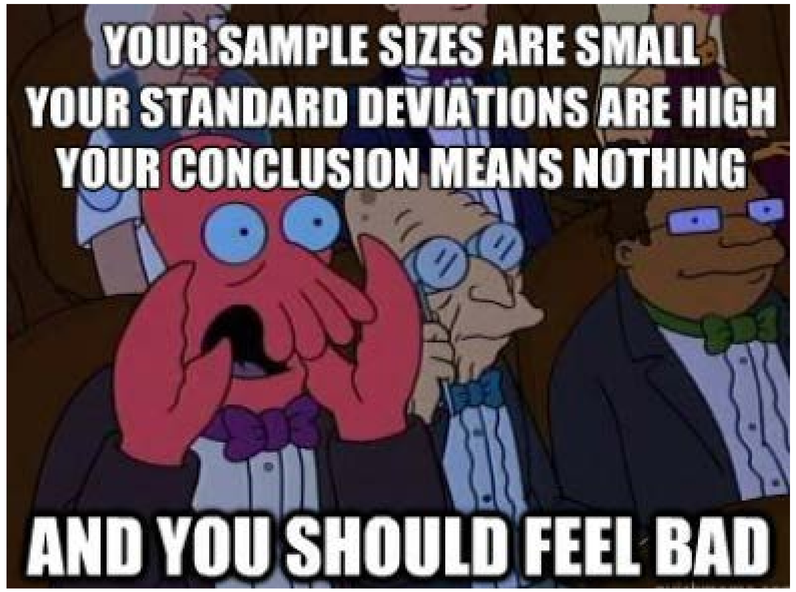
- If user-experienced bugs are the ones that matter, testing should be devoted to **sampling** those inputs that users will provide
- Two views:
  - Sample what users do most commonly
  - Sample what causes the most harm if users do it
- Compare:
  - Risk = (Prob. of Event) * (Damage if Event Occurs)

Sampling Error

- In statistics, **sampling error** is incurred when the statistical **characteristics** of a **population** are *estimated* from a subset, or sample, of that population.
  - "Our test suite is a sample of inputs that could occur in the real world. Our program behaves well on our test suite."
    → later →
    "Our program behaves badly on some other untested real input. Sampling error!"
- Testing gives confidence the same way sampling (or polling) gives confidence.

Sampling Bias

- In statistics, **sampling bias** is a bias in which a sample is collected in such a way that **some members** of the intended population are **less likely** to be **included** than others.
  - Suppose you are conducting a poll to see who will win the next election, but you only poll republicans.
  - Suppose you are creating tests to see if your program will crash,
    but you only poll nice, small, inputs.


YOUR SAMPLE SIZES ARE SMALL
YOUR STANDARD DEVIATIONS ARE HIGH
YOUR CONCLUSION MEANS NOTHING
AND YOU SHOULD FEEL BAD

Solution?

- There are a number of well-established sampling techniques in the field of statistics to help address such biases
  - They often require knowing something about the distribution of the full population from which you want to sample a subpopulation
- The basic problem in SE is that the underlying distribution of real user inputs **is not known**

Beta Testing

- **Alpha testing** is testing done by developers.
- **Beta testing** is testing done by external users (often using a special beta version of the program).
  - See also "Early Access"
- Beta testing can be viewed as directly sampling the space of user inputs

Steam "Early Access" Starterpack

10%

Not Recomm...
11.1 hrs on record (8...

RECENT REVIEWS: Mixed - 50% ...
ALL REVIEWS: Mostly Positiv...

EARLY ACCESS REVIEW POSTED: 26 OCTOBER
Nowhere near enough content to justify the price

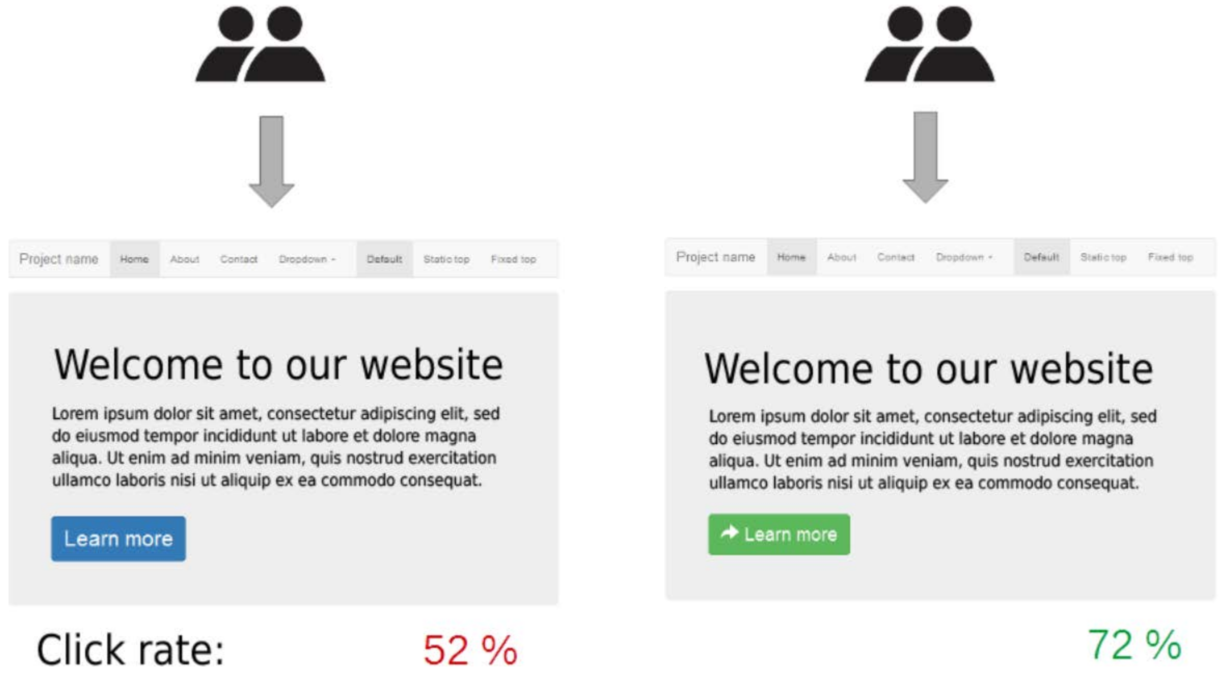
Game seems decent but basic stuff isn't there.
Options are way to limited. Can't even change key binds.

Patch 2.0.2 is live!

And when you will fix this problem?

A/B Testing

- **A/B testing** involves two variants of your software, A and B, which differ only in one feature. Different users are shown different variants and responses are recorded. It is an instance of two-sample statistical hypothesis testing.


Project name
Home
About
Contact
Dropdown
Default
Static top
Fixed top
Welcome to our website
Lorem ipsum dolor sit amet, consectetur adipiscing elit, sed do eiusmod tempor incididunt ut labore et dolore magna aliqua. Ut enim ad minim veniam, quis nostrud exercitation ullamco laboris nisi ut aliquip ex ea commodo consequat.
Learn more
Click rate:
52 %
72 %

Likely or Damaging?

- Recall two guiding approaches:
  - Sample what users will do most commonly
  - Sample what will cause the most harm
- The former is sometimes called **workload generation**
  - Common for databases, webservers, etc.
- The latter often relates to computer security
  - Exploit generation, penetration testing, etc.

Likely or Damaging?

- Recall two g
  - Sample wh
  - Sample wh
- The former ration
  - Common fc
- The latter
  - Exploit g

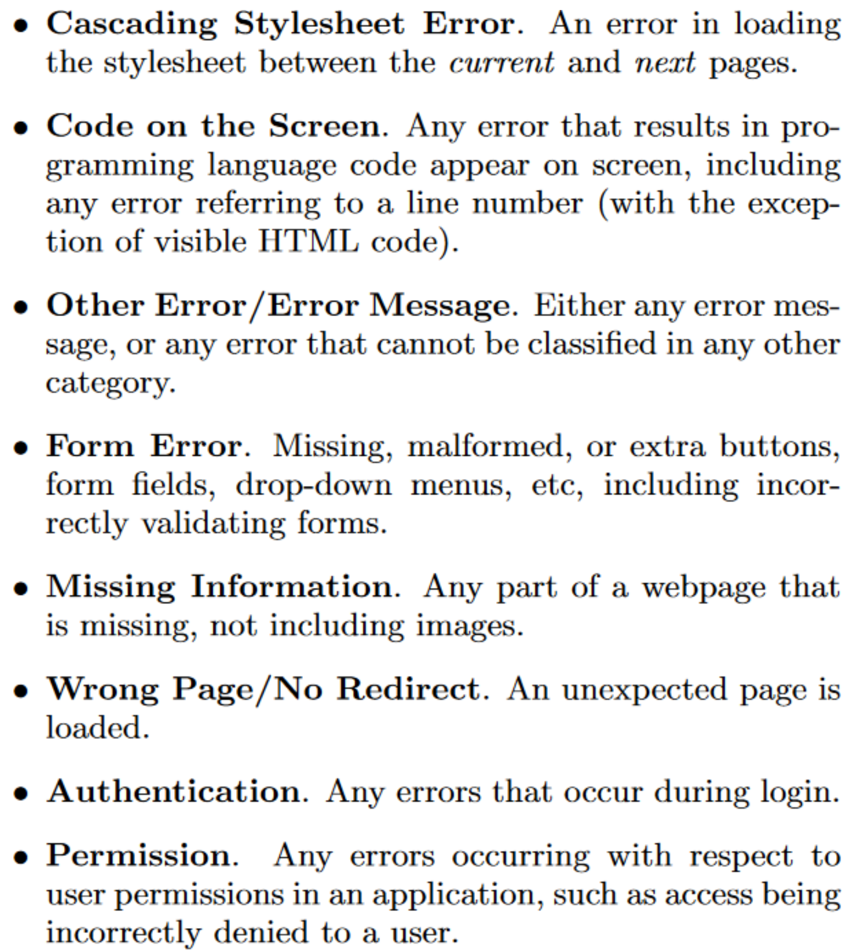
MYTH II: SOULBLIGHTER WANTED TO HARVEST YOUR COMPUTER'S SOUL

Thursday, July 5

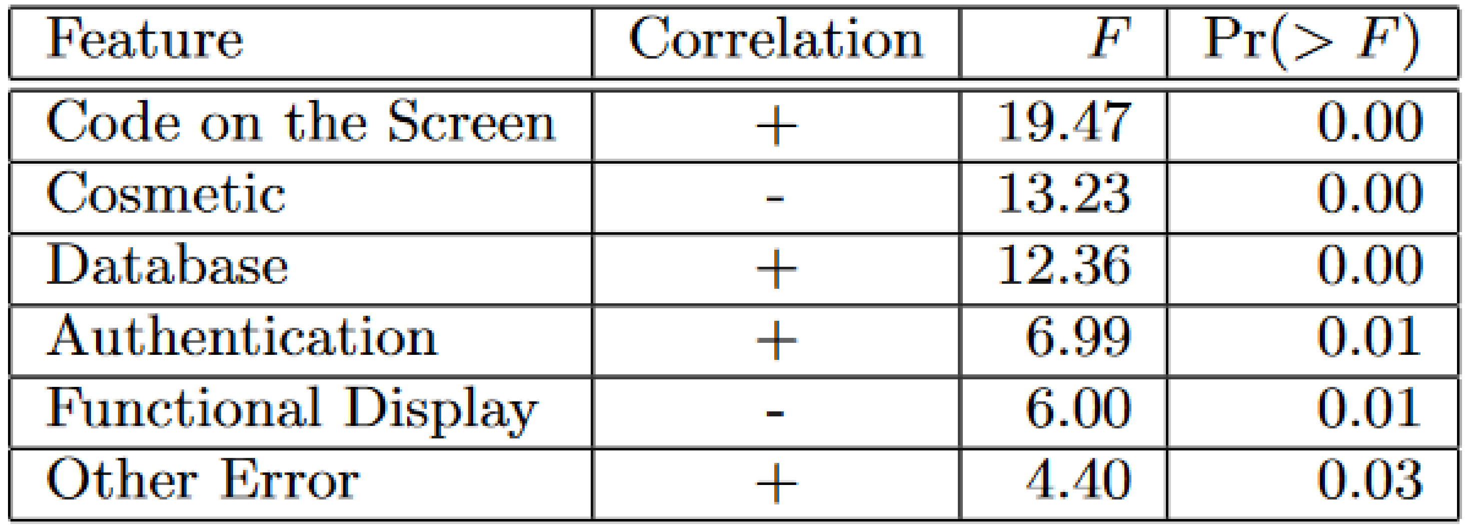
It turns out the uninstaller programme on the games's disc contained a particularly stupid coding oversight which deleted the entire contents of the folder where Soulblighter had been installed. If that happened to be the computer's root directory rather than the intended default location, uninstalling the game basically removed Windows and the rest of the content from the PC's hard drive thus creating a giant brick.

Non-Security Damage

- For Amazon (etc.), “damaging” is “customer does not complete the purchase”



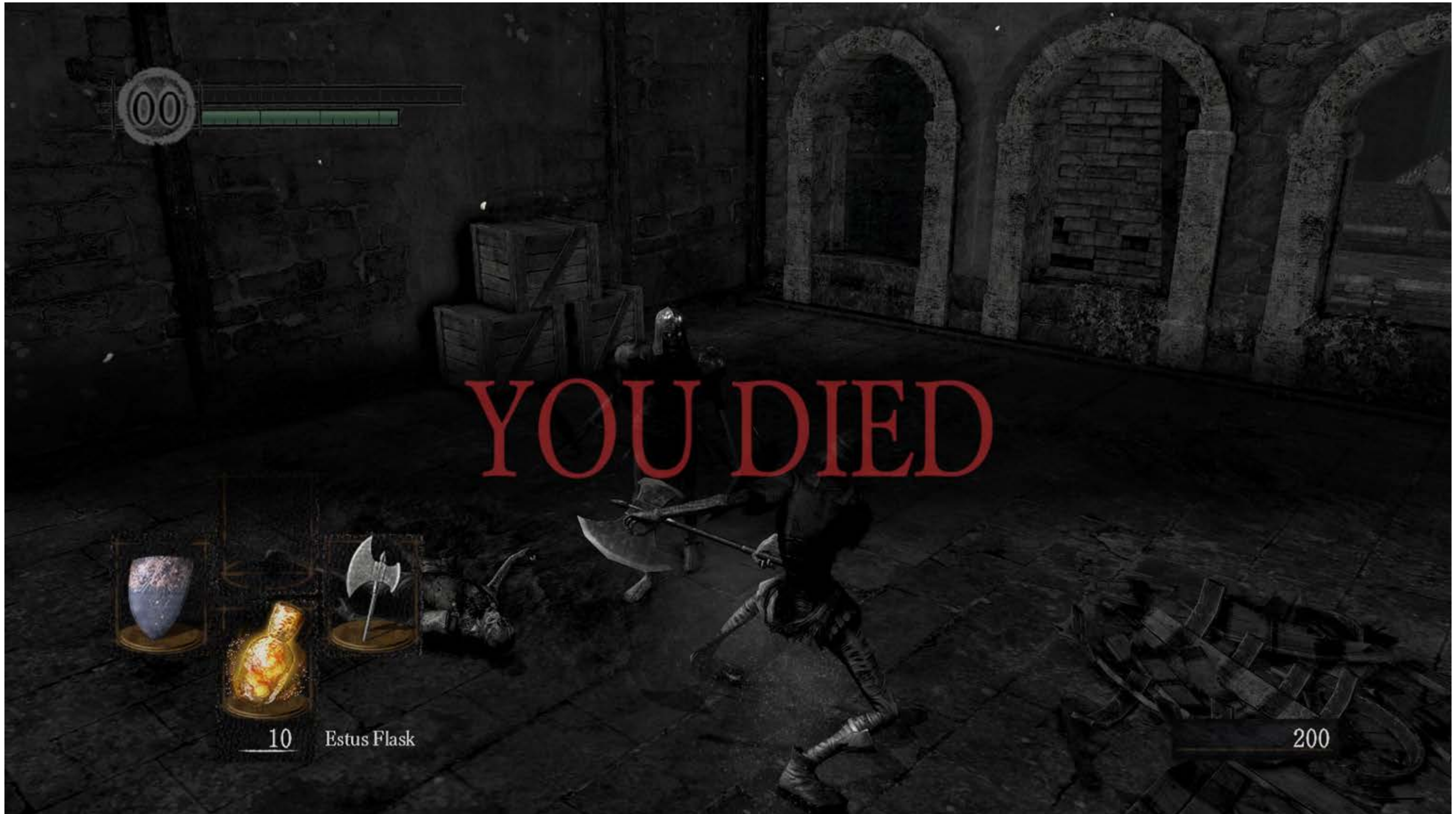
- **Cascading Stylesheet Error**. An error in loading the stylesheet between the *current* and *next* pages.
- **Code on the Screen**. Any error that results in programming language code appear on screen, including any error referring to a line number (with the exception of visible HTML code).
- **Other Error/Error Message**. Either any error message, or any error that cannot be classified in any other category.
- **Form Error**. Missing, malformed, or extra buttons, form fields, drop-down menus, etc, including incorrectly validating forms.
- **Missing Information**. Any part of a webpage that is missing, not including images.
- **Wrong Page/No Redirect**. An unexpected page is loaded.
- **Authentication**. Any errors that occur during login.
- **Permission**. Any errors occurring with respect to user permissions in an application, such as access being incorrectly denied to a user.



Feature	Correlation	F	$\Pr(> F)$
Code on the Screen	+	19.47	0.00
Cosmetic	-	13.23	0.00
Database	+	12.36	0.00
Authentication	+	6.99	0.01
Functional Display	-	6.00	0.01
Other Error	+	4.40	0.03

[Dobolyi et al. Modeling Consumer-Perceived Web Application Fault Severities for Testing. ISSTA 2010.]

Lens of Adversity



Finding Bugs

- Suppose you want to decide between two metal detectors
- You might bury some metal pieces in your yard
    - The metal detector that finds more of the pieces is expected to be better at finding metal in the wild
- Suppose you wanted to evaluate the quality of two bug-finding test suites …

Mutation Testing

- **Mutation testing** (or **mutation analysis**) is a test suite adequacy metric in which the quality of a test suite is related to the number of intentionally-added defects it finds.
- Informally: “You claim your test suite is really great at finding security bugs? Well, I'll just intentionally add a bug to my source code and see if your test suite finds it!”

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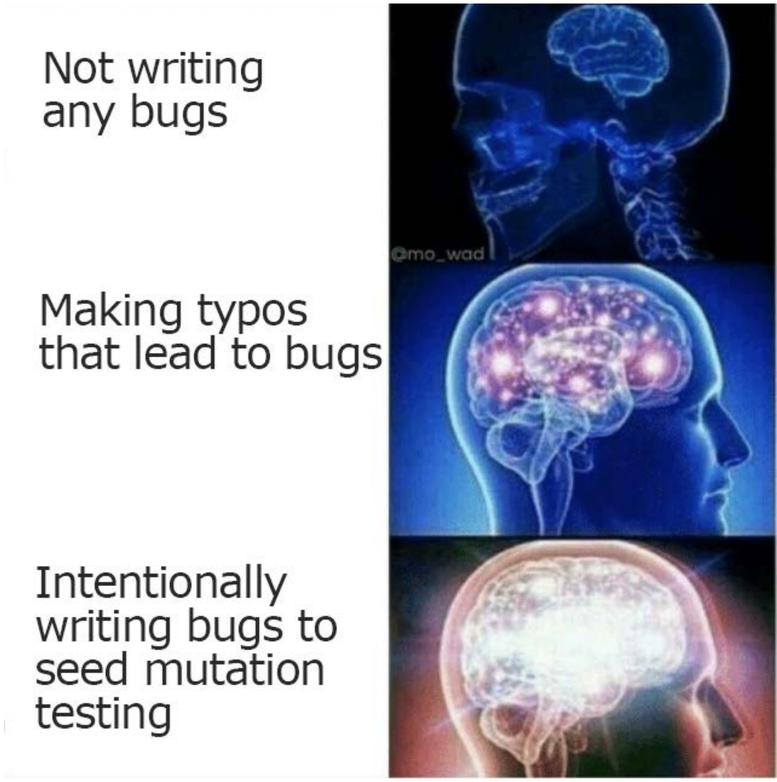
Verisimilitude

- In the metal detector example, if every piece of metal I bury is next to an underground pipe, the metal detector that finds them all may not actually do well in the real world
  - The metal placement I decided on was ***not indicative*** of metal in the real world
- Similarly, if I add a bunch of *defects* to my software that are *not at all the sort of defects real humans would make*, then mutation testing is uninformative

Defect Seeding

- **Defect seeding** is the process of *intentionally introducing* a defect into a program. The defect introduced is similar to defects introduced by *real developers*. The seeding is typically done by changing the **source code**.
- For mutation testing, defect seeding is typically done automatically (given a model of what human bugs look like)
    - You will do this in Homework 3


Not writing any bugs
@mo_wad
Making typos that lead to bugs
Intentionally writing bugs to seed mutation testing

Mutation Operators

- A **mutation operator** systematically changes a program point. In mutation testing, the mutation operators are modeled on historical human defects. Examples:
- `if (a < b)` → `if (a <= b)`
- `if (a == b)` → `if (a != b)`
- `a = b + c` → `a = b - c`
- `f(); g();` → `g(); f();`
- `x = y;` → `x = z;`

Mutant

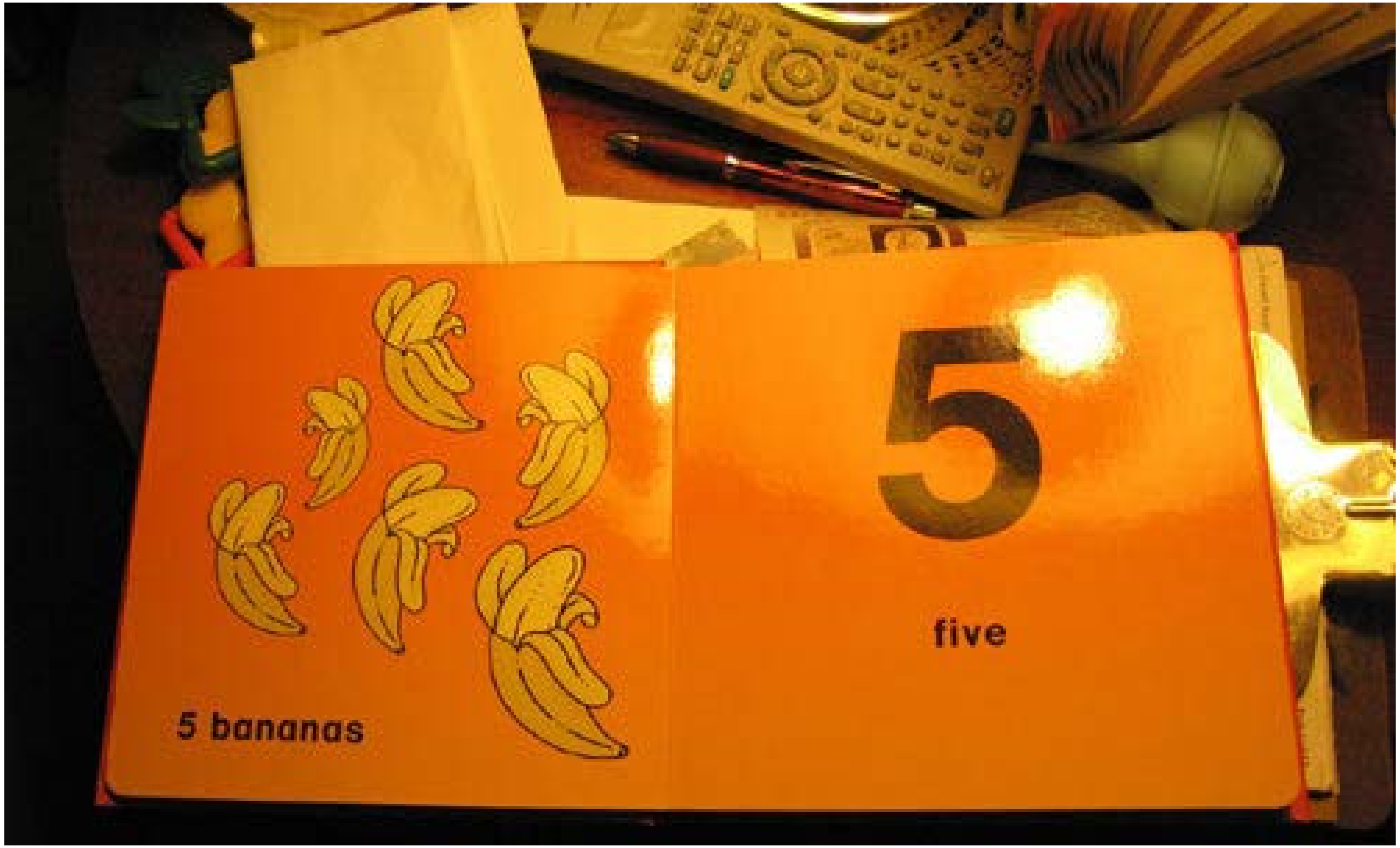
- A **mutant** (or **variant**) is a version of the original program produced by applying one or more mutation operators to one or more program locations. The **order** of a mutant is the number of mutation **operations** applied. Note: NOT the number of **operators** applied.

```
// original                        // 2nd-order mutant
if (a < b):                             if (a <= b):
  x = a + b          →                    x = a – b
  print(x)                                print(x)
```

Competent Programmers

- The **competent programmer hypothesis** holds that program faults are syntactically small and can be corrected with a few keystrokes.
- Programmers write programs that are largely correct. Thus the mutants simulate the likely effect of real faults. Therefore, if the test suite is good at catching the artificial mutants, it will also be good at catching the unknown but real faults in the program.

Do Humans Really Make Simple Mistakes?



Competent?

- Is the competent programmer hypothesis true?

```
// return true if x is greater
// than or equal to y
bool value_to_return;
if(x > y) {
  value_to_return = true;
}
if(x < y) {
  value_to_return = false;
}
if(x == y) {
  value_to_return = true;
}
return value_to_return;
```

Competent?

- Is the competent programmer hypothesis true?

- Yes and no.
- It is certainly true that humans often make simple typos (e.g., + to -).
- But it is also true that some bugs are more complex than that.

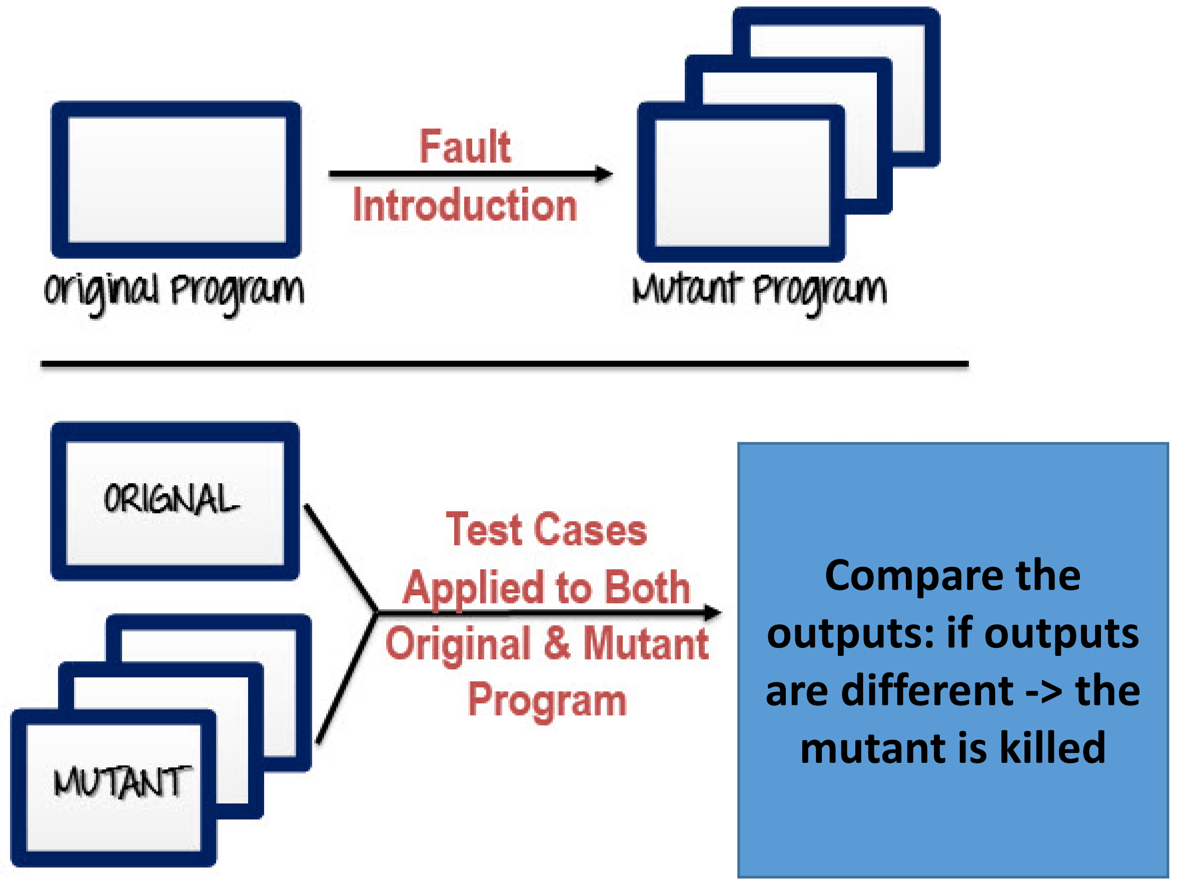
Coupling Effect

- The **coupling effect hypothesis** holds that complex faults are "coupled" to simple faults in such a way that a test suite that detects all simple faults in a program will detect a high percentage of the complex faults.
- Is it true?
    - Tests that detect simple mutants were also able to detect over 99% of second- and third-order mutants historically
      [A. J. Offutt. Investigations of the software testing coupling effect. ACM Trans. Softw. Eng. Methodol., 1(1):5–20, Jan. 1992.]

Mutation Testing

- A test suite is said to **kill** (or **detect**, or **reveal**) a mutant if the mutant fails a test that the original passes.
- **Mutation testing** (or **mutation analysis**) of a test suite proceeds by making a number of mutants and measuring the fraction of them killed by that test suite. This fraction is called the **mutation adequacy score** (or **mutation score**).
  - A test suite with a higher score is better.

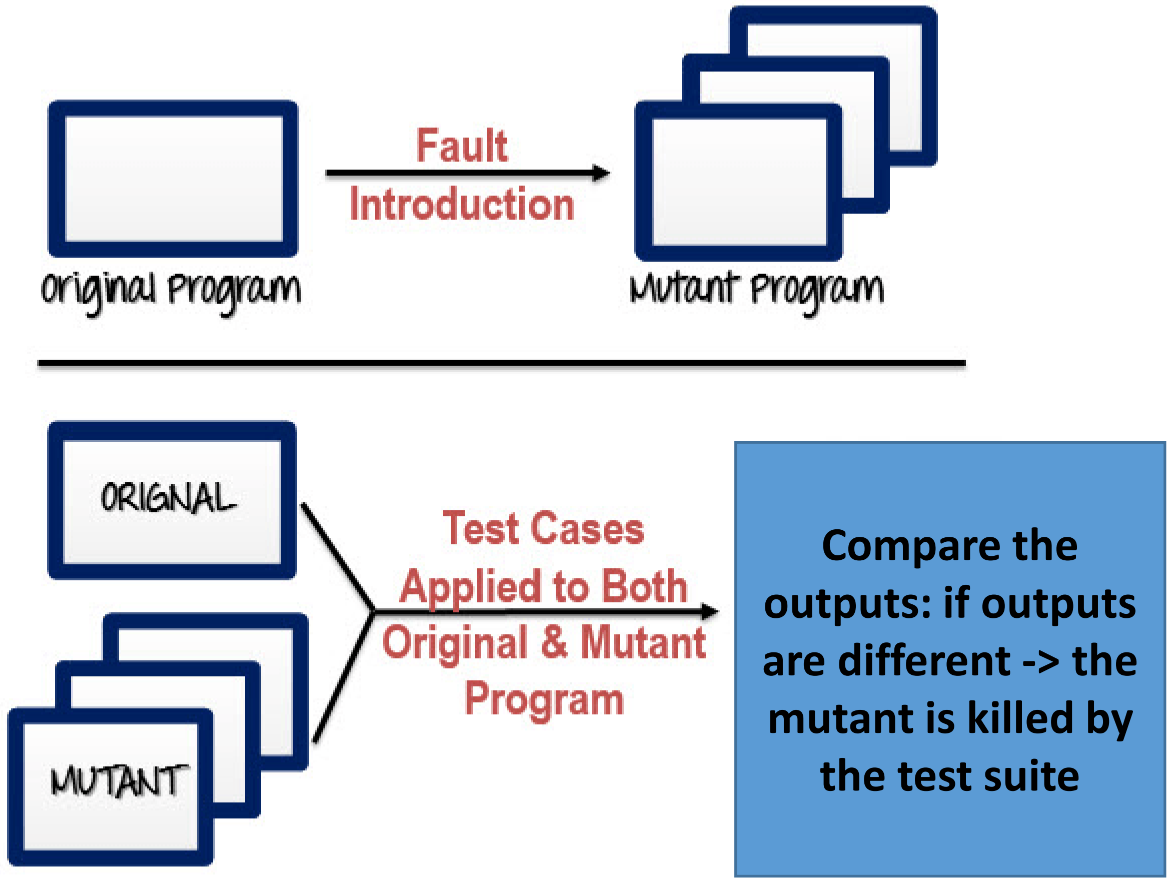
Mutation Testing


Original Program
Fault Introduction
Mutant Program
ORIGNAL
MUTANT
Test Cases Applied to Both Original & Mutant Program
Compare the outputs: if outputs are different -> the mutant is killed

Mutation Testing

- Mutation score =

number of mutants killed / total number of mutants * 100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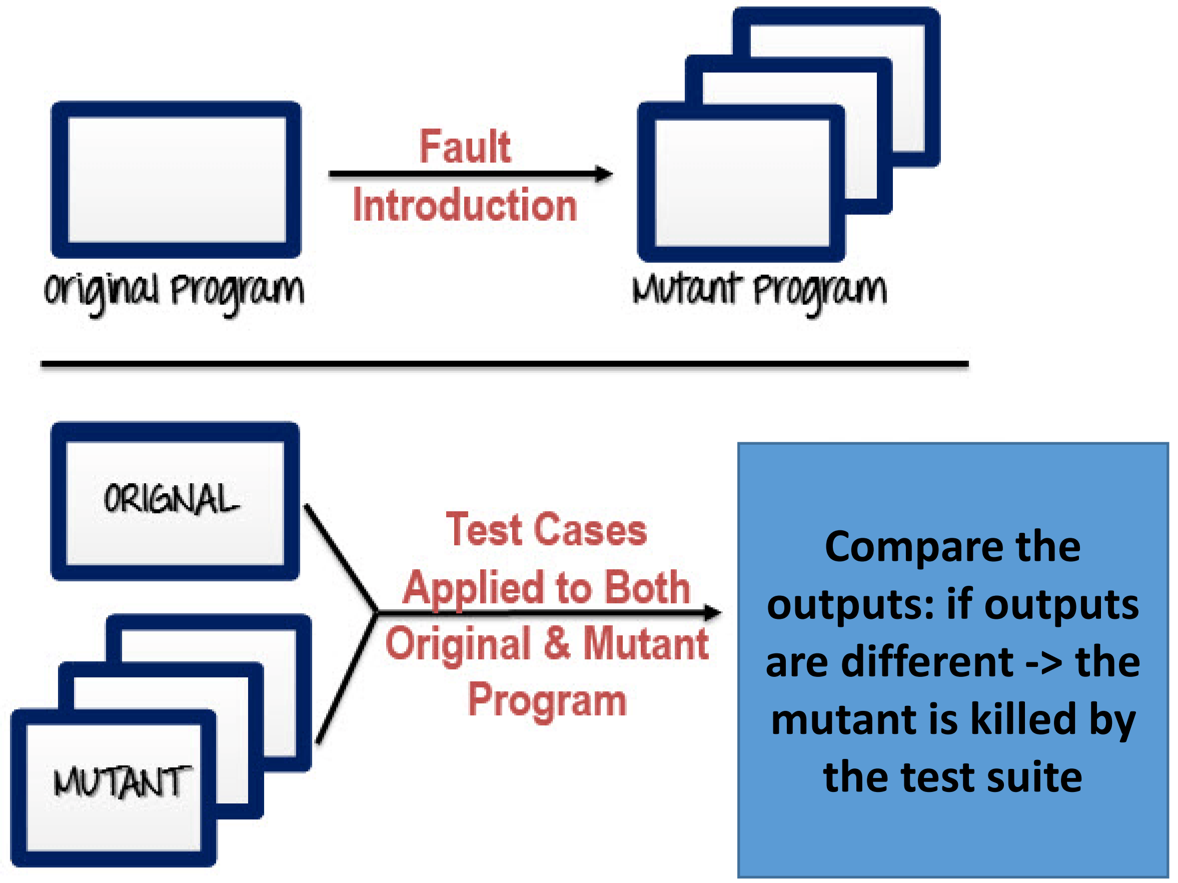
Mutation Testing

- Stillborn mutants
  - Syntactically incorrect, killed by compiler: e.g., x=a++b
- Trivial mutants
  - Killed by almost any test case
- Equivalent mutants → HARD
  - Always acts in the same behavior as the original program: e.g., x=a+b and x=a-(-b)

•None of the above is interesting.
•We care about mutants that behave differently but we don’t have test cases to identify them yet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Compare the outputs: if outputs are different -> the mutant is killed by the test suite

Equivalent Mutant Problem

- Suppose you have “x = a + b; y = c + d;” and you swap those two statements.
- The resulting program is a mutant, but it is semantically **equivalent** to the original.
    - So it will pass and fail all of the tests that the original passes and fails.
- So it will dilute the mutation score
- Detecting equivalent mutants is a big deal. How hard is it?

Equivalent Mutant Problem

- Detecting equivalent mutants is a big deal. How hard is it?
- It is **undecidable**!
  - By direct reduction from the halting problem (or by Rice's Theorem)

```
foo:                        # foo halts if and only if
  if p1() == p2():         # p1 is equivalent to p2
    return 0
  foo()
```

Mutation Analysis: Pros and Cons

- Has the potential to subsume other test suite adequacy criteria
  - Read: it can be very good
- Which mutation operators do you use?
- Where do you apply them? How often do you apply them?
  - Typically done at random, but how?
- It is **very expensive**. If you make 1,000 mutants, you must now run your test suite 1,000 times!
  - We started by saying testing (1x) was expensive!

Questions?

- Lens of Logic: “no visit X → no find bug in X”
  - Leads to statement and branch coverage.
- Lens of Statistics: “sample the inputs the users will make”
  - Leads to beta testing, A/B testing.
- Lens of Adversity: “poke realistic holes in the program and see if you find them”
  - Leads to mutation testing.